REV-01 BSC/01/05

B.SC. PHYSICS

FIRST SEMESTER INTRODUCTION TO MATHEMATICAL PHYSICS

BSP-101 [REPEAT]

(USE OMR FOR OBJECTIVE PART)

SET

2024/11

Duration: 3 hrs.

Objective

Time: 30 min.

Marks: 20

Choose the correct answer from the following:

 $1 \times 20 = 20$

Full Marks: 70

- 1. Curl grad $\vec{r} = ?$
 - a. 1

b. 0

e. 3

- d. ∞
- 2. $\nabla \times (\phi \vec{a})$, where Φ is a scalar field and \vec{a} is a vector field is given by
 - a. $\phi \vec{\nabla} \times \vec{a}$

b. $\nabla \vec{\phi} \times \vec{a}$

c. a×Vø

- d. $\nabla \vec{\phi} \times \vec{a} + \phi \vec{\nabla} \times \vec{a}$
- If a vector field $\vec{F} = x\hat{i} + 2y\hat{j} + 3z\hat{k}$, then $\nabla \times \nabla \times \vec{F}$ is
 - a. 0

e. 2 j

- d. $3\hat{k}$
- 4. Which of the following is axial vector?
 - a. momentum

b. displacement

e. torque

- d. force
- 5. What is a Laplacian operator?
 - a. second order differential operator
 - e. a complex operator

- b. first order differential operator
- d. null function
- 6. How to relate double integrals with line integrals in a plane
 - a. Green's Theorem

b. Stokes theorem

c. Gauss theorem

- d. Greens hypothesis
- 7. The Wronskian of two differentiable functions f and g is
 - a. W(f, g) = fg gf'

b. W(f, g) = f g' - g f

e. W(f, g) = g g' - f f'

- d. W(f, g) = f g' g f'
- 8. The magnitudes of two vectors are 3 and 4 units and their dot product is 6 units. The angle between the vectors is
 - а. п/6

b. n/3

с. п/2

d. n/4

- 9. ----- of gradient is a Laplacian operator. (Fill in the blank)
 - a. Divergence

b. Curl

c. Gradient

d. None of these

- 10. The gradient of a scalar quantity is a ----
 - a. vector function

b. vector field

c. Scalar function

d. Vector Potential

The electric field due to a point charge Q is expressed $\vec{E} = \frac{Q\hat{r}}{4\pi\varepsilon_0 r^2}$, then the

divergence of electric field due to that point charge is

a.
$$\frac{3Q}{4\pi\varepsilon_0 r^2}$$

b. $\frac{2Q}{4\pi\varepsilon_0 r}$

d. $\frac{3Q}{4\pi\varepsilon_0 r}$

- 12. Stoke's theorem is the relationship between
 - a. Surface and volume integral
 - c. line and volume integral
- b. line and surface integral
- d. none of these
- 13. Let \vec{F} be the force on a particle moving along \vec{C} . Then $\int_{C} \vec{F} \cdot d\vec{r}$ represents
 - a. velocity of the particle
 - c. work done by the force

- **b.** projection of \vec{F} in the direction of the position vector of the particle
- d. acceleration of the particle
- 14. What is the wronskian determinant of x^2, x^3
 - a. 2x4
 - c. 3 x4

- b. x⁴
 d. 4 x⁴
- 15. What is a first-order differential equation?
 - An equation involving derivatives of any order
 - An equation involving only the second derivative of a function
- An equation involving only the first derivative of a function
- d. An equation involving no derivatives
- 16. Which of the following is a first-order differential equation?
 - $a. \frac{d^2y}{dx^2} + y = 0$

b. $\frac{dy}{dx} + y = 0$

c. $\frac{d^3y}{dx^3} + \frac{d^2y}{dx^2} + y = 0$

d. None of these

- 17. Particular integral of $y'' + 2y' 3y = e^{2x}$ is
 - a. $-\frac{1}{5}e^{2x}$

- 18. The roots of the characteristic equation of $\frac{d^2y}{dx^2} + \frac{2dy}{dx} + 2y = 0$
 - a. Real and equal

b. Real and but not equal

c. Imaginary

- d. Undefined
- 19. For the right handed system of three coplanar vectors $\vec{A} = \hat{i} - \hat{j} - 2\hat{k}$,

$$\vec{B} = 3\hat{i} + 5\hat{j} + 6\hat{k}$$
, $\vec{C} = -\hat{i} + 4\hat{j} + m\hat{k}$, the value of m must be equal to

c. 6.5

- If $\vec{A} = x\hat{i}$ and $\vec{B} = y\hat{i}$ then $\nabla(\vec{A}.\vec{B})$ is equal to

a.
$$x\hat{i} + y\hat{j}$$

b.
$$\frac{1}{2}yx^2\hat{i} + \frac{1}{2}xy^2\hat{j}$$

d. 2

c. 0

Descriptive

Time: 2 hrs. 30 min.

Marks: 50

[Answer question no.1 & any four (4) from the rest]

- 1. **a.** Find the value of $\nabla \cdot (\frac{a \times r}{|r|^n})$, where $r = x\hat{i} + y\hat{j} + z\hat{k}$. 5+5=10 **b.** Solve $\frac{d^2y}{dx^2} + 6y = \sin 4x$
- 2. a. If four vectors whose position vectors are $\vec{a}, \vec{b}, \vec{c}$ are coplanar, 5+5=10 show that $[\vec{a}\vec{b}\vec{c}] = [\vec{a}\vec{d}\vec{b}] + [\vec{a}\vec{d}\vec{c}] + [\vec{d}\vec{b}\vec{c}]$

- **b.** An equation relating to stability of an areoplane is $\frac{dv}{dt} = g \cos \alpha kv, \text{ where } v \text{ is the velocity, } g,a,k \text{ being constants. Find an expression for the velocity if } v=0 \text{ when } t=0.$
- 3. State Green's theorem. (a) Using Green's theorem, evaluate $\int_{c} (x^2ydx + x^2dy)$, where c is the boundary described counter clockwise of the triangle with vertices (0,0), (1,0), (1,1). (b) A vector field F is given by F=sinyi+x(1+cosy)j. Evaluate the line integral $\int_{c} \mathbf{F}.d\mathbf{r}$, where c is the circular path given by $x^2 + y^2 = a^2$
- 4. **a.** Evaluate $\nabla^2(\ln r)$. 6+4=10 **b.** Prove that $\hat{i} \times (\vec{a} \times \hat{i}) + \hat{j} \times (\vec{a} \times \hat{j}) + \hat{k} \times (\vec{a} \times \hat{k}) = 2\vec{a}$
- 5. State Gauss's Divergence theorem. Evaluate $\iint \vec{A} \cdot \hat{n} dS$, where $\vec{A} = 18z\hat{i} 12\hat{j} + 3y\hat{k}$ and S is that part of the plane 2x + 3y + 6z = 12 which is located in the first octant.
- 6. Solve a. $(D^2 - 4D + 4)Y = 2x^3e^{2x}$ b. $(D^3 + 1)y = e^{-x}$
- 7. **a.** Prove that for every vector field \vec{V} , $div(curl\vec{V}) = 0$. **b.** Show that $div(grad\ r^n) = n(n+1)r^{n-2}$, where $r = (x^2 + y^2 + z^2)^{1/2}$
- 8. Solve 5+5=10a. $(1+x^2)dy xydx = 0$ b. Find the value of λ for the differential equation
 - **b.** Find the value of λ , for the differential equation $(xy^2 + \lambda x^2 y)dx + (x + y)x^2 dy = 0$ is exact.

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