

**B.Sc. PHYSICS**  
**FIRST SEMESTER**  
**MATHEMATICAL PHYSICS-I**  
**BSP – 101 OLD COURSE [REPEAT]**  
[USE OMR FOR OBJECTIVE PART]

**SET**  
**A**

Duration: 3 hrs.

Full Marks: 70

Time: 30 min.

Marks: 20

**[ Objective ]**

**1×20=20**

**Choose the correct answer from the following:**

1. If  $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$  and  $|\vec{r}| = r$ , then  $\text{div } \vec{r}$  is  
a. 2  
b. 3  
c. -3  
d. -2
2. For the right handed system of three coplanar vectors  
 $\vec{A} = \hat{i} - \hat{j} - 2\hat{k}$ ,  $\vec{B} = 3\hat{i} + 5\hat{j} + 6\hat{k}$ ,  $\vec{C} = -\hat{i} + 4\hat{j} + m\hat{k}$ , the value of m must be equal to  
a. 5  
b. 8  
c. 0  
d. 6.5
3. A vector points A vertically upward and point B towards north. The vector product  $\mathbf{A} \times \mathbf{B}$  is  
a. along west  
b. along east  
c. zero  
d. vertically downward
4. The unit normal to  $x^2 + y^2 + z^2 = 5$  at the point (0,1,2) is  
a.  $\frac{1}{\sqrt{5}}(\hat{i} + \hat{j} + \hat{k})$   
b.  $\frac{1}{\sqrt{5}}(\hat{i} + \hat{j} - \hat{k})$   
c.  $\frac{1}{\sqrt{5}}(\hat{i} + 2\hat{k})$   
d.  $\frac{1}{\sqrt{5}}(\hat{i} - \hat{j} + \hat{k})$
5. Gauss's theorem is the relationship between  
a. Surface and volume integral  
b. line and surface integral  
c. line and volume integral  
d. none of these
6. If  $\phi = yz$ , then its gradient is  
a.  $z\hat{j} + y\hat{k}$   
b. 0  
c.  $y\hat{j} + z\hat{k}$   
d.  $\hat{i} + \hat{j} + \hat{k}$

7. The electric field due to a point charge Q is expressed  $\vec{E} = \frac{Q\hat{r}}{4\pi\epsilon_0 r^2}$ , then the divergence of electric field due to that point charge is
- $\frac{3Q}{4\pi\epsilon_0 r^2}$
  - $\frac{2Q}{4\pi\epsilon_0 r}$
  - 0
  - $\frac{3Q}{4\pi\epsilon_0 r}$
8. The direction of  $\text{grad}\phi$  is
- Tangential to level surfaces
  - Normal to level surface
  - Inclined at  $45^\circ$  to level surface
  - Arbitrary
9. If  $\vec{A} = x\hat{i}$  and  $\vec{B} = y\hat{j}$  then  $\nabla(\vec{A} \cdot \vec{B})$  is equal to
- $x\hat{i} + y\hat{j}$
  - 0
  - $\frac{1}{2}yx^2\hat{i} + \frac{1}{2}xy^2\hat{j}$
  - 2
10. The flux leaving any closed surface per unit volume in a vector field  $\vec{A}$  is called
- $\text{grad } \vec{A}$
  - $\text{div } \vec{A}$
  - $\text{curl } \vec{A}$
  - $\text{flux } \vec{A}$
11. Which of the following vectors are perpendicular to each other?
- (i)  $2\hat{i} - 2\hat{j} + 4\hat{k}$ , (ii)  $10\hat{i} + 8\hat{j} + 12\hat{k}$  and (iii)  $3\hat{i} + 11\hat{j} + 4\hat{k}$
- (i) And (ii)
  - (ii) And (iii)
  - (iii) And (i)
  - None of these
12. If for two vectors  $\vec{a}$  and  $\vec{b}$ ,  $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$  then angle between  $\vec{a}$  and  $\vec{b}$  is
- 0
  - $\frac{\pi}{2}$
  - $\frac{\pi}{4}$
  - $\frac{\pi}{3}$



13. If  $\vec{F} = \text{grad}(2x^2 - 3y^2 + 4z^2)$ , then  $\text{curl } \vec{F}$  is
- a.  $4x\hat{i} - 6y\hat{j} + 8z\hat{k}$                       b.  $4x\hat{i} - 6y\hat{j} + 8z\hat{k}$   
 c. 0    d. 3
14. Order of differential equation whose solution  $y = ae^x + be^{2x} + ce^{3x}$  will be
- a. 1    b. 2  
 c. 3    d. 0
15.  $\frac{1}{f(D)}x^m$  will be equal to
- a.  $[F(D)]^{-1}x^m$                               b.  $F(D)x^m$   
 c.  $mF(D)x^{m-1}$                               d.  $mx^{m-1}[F(D)]^{-1}$
16. What is the wronskian determinant of  $x^2, x^3$
- a.  $2x^4$     b.  $x^4$   
 c.  $3x^4$     d.  $4x^4$
17. The value of  $\alpha$  so  $e^{\alpha y^2}$  that is an I.F. of the equation  $(e^{-y^2} - xy)dy - dx = 0$
- a. -1    b. 1  
 c.  $\frac{1}{2}$     d.  $-\frac{1}{2}$
18. General solution of linear differential equation of first order  $\frac{dx}{dy} + Px = Q$
- a.  $ye^{\int P dx} = \int Qe^{\int P dx} dx + C$                       b.  $xe^{\int P dy} = \int Qe^{\int P dy} dy + C$   
 c.  $y = \int Qe^{\int P dx} dx + C$                       d.  $x = \int Qe^{\int P dy} dy + C$
19. Particular integral of  $y'' + 2y' - 3y = e^{2x}$  is
- a.  $-\frac{1}{5}e^{2x}$                                       b.  $\frac{1}{5}e^{2x}$   
 c.  $-\frac{1}{5}$     d.  $-\frac{1}{5}$

20. When  $y = f(x) + c g(x)$  is the solution of an ordinary differential equation then
- |   |  |
|---|--|
| a. $f$ is called the particular integral (P.I.) and $g$ is called the complementary function (C.F.) | b. $f$ is called the complementary function (C.F.) and $g$ is called the particular integral (P.I.). |
| c. $f$ is called the complementary function (C.F.) and $g$ is called the particular function (P.I.) | d. $g$ is called the complementary function (C.F.) and $g$ is called the particular function (P.I.)  |

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**( Descriptive )**

Time : 2 hrs. 30 mins.

Marks : 50

*[ Answer question no.1 & any four (4) from the rest ]*

1. a. Define Wronskian. 2+2+4+  
2=10
- If  $y_1 = e^{-x} \cos x$ ,  $y_2 = e^{-x} \sin x$
- b. Find Wronskian determinant.
- c. Verify that the solutions satisfy the differential equation
- $$\frac{d^2 y}{dx^2} + \frac{2dy}{dx} + 2y = 0.$$
- d. Show by Wronskian test the solutions are independent.
2. Solve 5+5=10
- a.  $\frac{d^2 y}{dx^2} - 2 \frac{dy}{dx} + y = xe^x \sin x$
- b. Solve the differential equation  $\frac{d^2 x}{dt^2} + \frac{g}{l} x = \frac{g}{l} L$   
where  $g, l, L$  are constants subject to the conditions  
 $x = a, \frac{dx}{dt} = 0$  at  $t = 0$ .



3. Solve 3+4+3  
=10

a.  $(x + 2y)(dx - dy) = dx + dy$

b.  $\frac{dy}{dx} = \frac{y+1}{(y+2)e^x - x}$

c. Find the value of  $\lambda$ , for the differential equation  $(xy^2 + \lambda x^2 y)dx + (x + y)x^2 dy = 0$  is exact.

4. a. Prove that the altitudes of a triangle are concurrent. 4+4+2  
=10

b. Find the value of  $n$  for which the vector  $r^n \vec{r}$  is solenoidal, where  $r = x\hat{i} + y\hat{j} + z\hat{k}$ .

c. Define curl of a vector function.

5. Define Laplacian operator in curvilinear co-ordinate system. Deduce an expression for gradient of a continuously differentiable vector point function in a curvilinear coordinates. 2+8=10

6. State Stoke's theorem. Verify Stoke's theorem for  $\vec{F} = (2x - y)\hat{i} - yz^2\hat{j} - y^2z\hat{k}$ , where S is the upper half surface of the sphere  $x^2 + y^2 + z^2 = 1$  and c is its boundary. 2+8=10

7. a. If  $\vec{A} = (3x^2 + 6y)\hat{i} - 14yz\hat{j} + 20xz^2\hat{k}$ , evaluate the  $\oint \vec{A} \cdot d\vec{r}$  from (0, 0, 0) to (1, 1, 1) along the curve C. 2+4+4=  
10

b. Evaluate  $\iint (yz\hat{i} + zx\hat{j} + xy\hat{k}) \cdot d\vec{s}$  where S is the surface of the sphere  $x^2 + y^2 + z^2 = a^2$  in the first octant.

c. If  $\vec{F} = (2x^2 - 3z)\hat{i} - 2xy\hat{j} - 4x\hat{k}$ , the evaluate  $\iiint \nabla \times \vec{F} \cdot d\vec{V}$ , where V is the closed region bounded by the planes  $x = 0, y = 0, z = 0$  and  $2x + 2y + z = 4$ .

8. a. Establish the relation  $\text{curl curl } \vec{f} = \nabla \text{div } \vec{f} - \nabla^2 \vec{f}$   
b. Prove that  $[\mathbf{a}+\mathbf{b}, \mathbf{b}+\mathbf{c}, \mathbf{c}+\mathbf{a}] = 2[\mathbf{a}, \mathbf{b}, \mathbf{c}]$ .

7+3=10

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