

M.Sc. PHYSICS  
SECOND SEMESTER  
MATHEMATICAL PHYSICS-I  
MSP – 201 [REPEAT]  
[USE OMR FOR OBJECTIVE PART]

**SET  
A**

Duration: 3 hrs.

Full Marks: 70

Time: 30 min.

( Objective )

Marks: 20

Choose the correct answer from the following:

1 × 20 = 20

1. If the Laplace transform of  $F(x)$  is  $f(s)$  (i.e.  $L[F(x)] = f(s)$ ), then  $L[e^{ax} \sin(ax)]$  is

a.  $\frac{a}{(s-a)^2 + a^2}$

b.  $\frac{a}{(s-a)^2 - a^2}$

c.  $\frac{s}{(s-a)^2 + a^2}$

d.  $\frac{s}{(s-a)^2 - a^2}$

2. If  $(1 - 2xh + h^2)^{-1/2} = \sum h^n p_n(x)$  then  $p_3(-1)$  will be

a. -1  
c. 0

b. 1  
d. -2

3. Inverse Laplace transform of  $\frac{s}{s^2 + a^2}$  is

a.  $\cos at$   
c.  $\sinh at$

b.  $\cosh at$   
d.  $\sin at$

4. The value of  $H_1\left(-\frac{1}{2}\right)$  will be

a. 1  
c. 0

b. 2  
d. -1

5. If  $\{F(t)\} = \bar{f}(s)$ , then  $L\left\{\int_0^t F(x) dx\right\}$  is

a.  $\int_0^s \bar{f}(s) ds$

b.  $\int_0^s \frac{1}{s} \bar{f}(s) ds$

c.  $\frac{1}{s} \bar{f}(s) ds$

d.  $s \bar{f}(s) ds$

6. The coefficient of  $h^1$  in the function  $(1 - 2xh + h^2)^{-1/2}$  will be
- $x$
  - $-x$
  - $-2x$
  - $x/2$
7. Fourier cosine transform of  $\frac{1}{\sqrt{x}}$
- $\sqrt{\frac{\pi}{2s}}$
  - $\sqrt{\frac{\pi}{s}}$
  - $\sqrt{\frac{2\pi}{s}}$
  - $\frac{1}{\sqrt{s}}$
8. The Bessel function of first kind  $J_{\frac{1}{2}}\left(\frac{\pi}{2}\right)$  will be
- $\frac{\pi}{2}$
  - $\frac{\pi}{4}$
  - $\frac{2}{\pi}$
  - $\frac{4}{\pi}$
9.  $F_s[f(ax)] = ?$
- $\frac{1}{a}F_s\left(\frac{s}{a}\right)$
  - $F_s\left(\frac{s}{a}\right)$
  - $\frac{1}{a}F_s(sa)$
  - $\frac{s}{a}F_s\left(\frac{s}{a}\right)$
10. The values of  $L_1\left(\frac{3}{2}\right)$  will be
- $\frac{1}{2}$
  - $-\frac{1}{2}$
  - $\frac{3}{2}$
  - 0
11. Find the dummy index in  $\delta_{im}^{ijk}$
- j
  - k
  - i
  - m
12. The expression  $H_1(x) - 2xH_0(x)$  in terms of  $x$  will be
- $2x$
  - $x - 2$
  - 0
  - $2x - 2$
13.  $\delta_j^i \delta_k^j = ?$
- $\delta_j^i$
  - $\delta_k^i$
  - $\delta_i^k$
  - $\delta_i^i$



**(Descriptive)**

Time : 2 hrs. 30 mins.

Marks : 50

*[ Answer question no.1 & any four (4) from the rest ]*

1. What is Bessels' equation? Obtain a polynomial solution  $J_n(x)$  of the Bessel's equation. 2+8=10
  
2. Solve the following equation by Laplace transform 10  
 $y''' - 2y'' + 5y' = 0$ ;  $y = 0$ ,  $y' = 1$  at  $t=0$  and  $y = 1$  at  $t = \frac{\pi}{8}$ .
  
3. a. Find Hermite polynomial expression  $H_3(x)$  using Rodrigue's formula. 3+4+3=10  
b. Express the function  $f(x) = 2x^2 - x + 4$  in terms of Hermite polynomial.  
c. Show that Hermite polynomial  $H_n(x)$  satisfies the following recurrence relation:  $2n H_{n-1}(x) = H'_n(x)$ .
  
4. a. Obtain Laplace transform of derivative for order 'n'. 5+5=10  
b. Find the Laplace transform of  $F(t) = \begin{cases} 1, & 0 \leq t < 1 \\ t, & 1 \leq t < 2 \\ t^2 & 2 \leq t < \infty \end{cases}$
  
5. a. Define Voltera Integral equation (VIE) of the first and second kind. 4+6=10  
b. Reduce the boundary value problem to the Voltera Integral equation:  
 $y''(x) + x y(x) = 1$ , where  $y(0) = 0$  and  $y'(0) = 1$ .
  
6. a. If  $a_{\alpha\beta} x^\alpha x^\beta = 0$  for all values of the variables  $x^1, x^2, x^3, \dots, x^n$ , then show that  $a_{\mu\theta} + a_{\theta\mu} = 0$  5+5=10

b. If  $A^\mu$  and  $B_\nu$  are the components of a contravariant and covariant tensors of rank one, show that  $C^\mu_\nu = A^\mu B_\nu$  are the components of a mixed tensor of rank two.

7. a. Show that Legendre polynomial  $p_n(x)$  satisfies the following orthogonality condition 6+4=10

$$\int_{-1}^1 p_n(x)p_m(x)dx = 0, n \neq m.$$

b. Express  $p_2(x) + 2p_1(x) - 3p_0(x)$  in terms of a polynomial function  $x$ .

8. a. Find the Fourier transform of the function 5+5=10

$$f(x) = \begin{cases} 1 + \frac{x}{a} & \text{for } -a < x < 0 \\ 1 - \frac{x}{a} & \text{for } 0 < x < a \\ 0 & \text{otherwise} \end{cases}$$

b. Find the Fourier sine transformation of  $\frac{1}{x}$ .

== \*\*\* ==