

B.S.C. PHYSICS
SECOND SEMESTER
MATHEMATICAL PHYSICS II
BSP – 202 [REPEAT]
[USE OMR FOR OBJECTIVE PART]

Duration: 1:30 hrs.



Full Marks: 35

Time: 15 mins.

(Objective)

Marks: 10

Choose the correct answer from the following: **$1 \times 10 = 10$**

1. The element a_{21} in the matrix $A = \begin{pmatrix} 3 & 1 \\ -1 & 2 \end{pmatrix}$ will be
 - a. 1
 - b. -1
 - c. 3
 - d. 2
2. If $A = \begin{pmatrix} 3 & -2 \\ 1 & 0 \end{pmatrix}$ then $2a_{21} + a_{12}$ will be
 - a. 1
 - b. -2
 - c. 0
 - d. 3
3. If $A = (a_{ij})_{2 \times 2} = \begin{pmatrix} 2 & 1 \\ -1 & 5 \end{pmatrix}$ then the co-factor of a_{22} will be
 - a. 1
 - b. -1
 - c. 2
 - d. 5
4. If $A = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$ and $B = (2 \quad 1)$, then BA will be
 - a. 0
 - b. -1
 - c. 1
 - d. 2
5. If $A = \begin{pmatrix} 1 & -1 \\ -2 & 3 \end{pmatrix}$ and $\det(A)$ will be
 - a. 1
 - b. 2
 - c. -1
 - d. 3
6. If $A = \begin{pmatrix} 1 & -1 \\ -2 & 2 \end{pmatrix}$ and $B = \begin{pmatrix} 1 & 1 \\ 2 & 0 \end{pmatrix}$, then $\frac{1}{2}(A + B)$ will be a matrix of what?
 - a. $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
 - b. $\begin{pmatrix} 0 & 2 \\ 2 & 0 \end{pmatrix}$
 - c. $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
 - d. $\begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix}$

— — —

(Descriptive)

Time : 1 hr. 15 min.

Marks : 25

[Answer question no.1 & any two (2) from the rest]

1. For the matrix $A = \begin{pmatrix} 2 & -1 \\ 3 & 5 \end{pmatrix}$, find its co-factor and determinant. 5

2. a. What do you mean by a symmetric and skew-symmetric matrix? 4+6=10
 b. Show that any square matrix can be expressible in terms of its symmetric and skew-symmetric parts.

3. a. If $I = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ and $C = \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}$, show that $(aI + bC)^3 = a^3I + 3a^2bC$. 5+5=10
 b. If $A = \begin{pmatrix} 4 & 2 \\ -1 & 1 \end{pmatrix}$, find $(A - I)(A - 2I)$.

4. a. If $A = \begin{pmatrix} 3 & -4 \\ 1 & -1 \end{pmatrix}$, then show that $A^n = \begin{pmatrix} 1+2n & -4n \\ n & 1-2n \end{pmatrix}$ for any positive integer n . 5+5=10
 b. If $A = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$, then find the expression $A^2 - 2A + I$.

5. a. What do you mean by Hermitian matrix? If A is a skew-Hermitian matrix then show that iA is Hermitian. 4+3+3=10
 b. Find transpose conjugate of the following matrices
 (i) $\begin{pmatrix} 1 & 2+3i \\ 2-3i & -2 \end{pmatrix}$ (ii) $\begin{pmatrix} 1+i & -1+2i \\ 1-i & 2 \end{pmatrix}$

$= * * * = =$