

**BACHELOR OF COMPUTER APPLICATION  
SECOND SEMESTER  
DISCRETE MATHEMATICS  
BCA-203**

(Use separate answer scripts for Objective & Descriptive)

Duration : 3 hrs.

Full Marks : 70

[ **PART-A : Objective** ]

Time : 20 min.

Marks : 20

*Choose the correct answer from the following:*

**1X20=20**

7. a. From a group consisting of 6 boys and 7 girls, in how many ways can we select a group of 8+2=10
- 3 boys and 4 girls
  - 4 persons which has atleast one girl.
  - 4 persons which has atleast one boy.
  - 4 persons that has both boys and girls.
- b. Prove by mathematical method  $n! \geq 2^{n-1}$ , for  $n = 1, 2, 3 \dots$

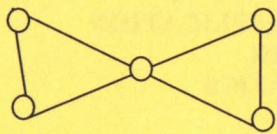
8. a. Define proposition with an example. 2+6+2=10
- b. Define conjunction and disjunction for any two propositions  $p$  and  $q$ . Construct the truth table for both the connectives.
- c. Write down the primal and dual form of the idempotent law and identity law.

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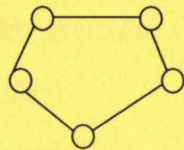
- A function  $f: X \rightarrow Y$  is a one-one function if
  - $f(x_1) = f(x_2)$  whenever  $x_1 = x_2$
  - $f(x_1) = f(x_2)$  whenever  $x_1 \neq x_2$
  - $f(x_1) \neq f(x_2)$  whenever  $x_1 = x_2$
  - None of these
- If  $A = \{1, 2, 3\}$  and  $B = \{w, x, y, z\}$ , then the number of functions  $f: A \rightarrow B$  is:
  - 64
  - 81
  - 12
  - None of these.
- The function  $f: \mathbb{Z} \rightarrow \mathbb{N}$  defined as  $f(x) = \begin{cases} 2x - 1, & \text{if } x > 0 \\ -2x, & \text{if } x \leq 0 \end{cases}$ . Then the value of  $f(1)$  and  $f(-1)$  are:
  - 1 and -2
  - 1 and 2
  - 1 and -2
  - None of these
- The function  $f: A \rightarrow A$  defined as  $f(x) = x$  where  $x \in A$  is a
  - Constant function
  - Identity function
  - Both (a) and (b)
  - None of these
- Consider the following statement:  
P: A graph with  $n$  vertices and  $n - 1$  edges is called tree.  
Q: A tree is a connected graph.
  - Only P is true.
  - Only Q is true
  - Both P and Q are true
  - Both P and Q are false.
- The chromatic number of  $C_5$  and  $C_6$  are:
  - 5 and 6 respectively.
  - 2 and 3 respectively
  - 3 and 2 respectively
  - None of these.
- Consider the following statement:  
P: Every tree with two or more vertices has chromatic number 2.  
Q: Chromatic number of  $K_n$  is  $n$ .
  - P is true, Q is false
  - P is false, Q is true
  - P and Q are true.
  - None of these.
- A graph with 8 vertices and 6 faces. Then the number of edges of the graph is:
  - 14
  - 12
  - 16
  - None of these
- The order of  $-1$  in the group  $G = \{1, -1, i, -i\}$  with respect to multiplication is
  - 1
  - 2
  - 3
  - 4

10. Which of the following graph has Hamiltonian path but not Hamiltonian cycle?

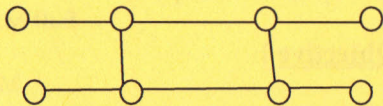
a.



b.



c.



d. None of these

11. Which of the following is true?

a.  $P(n, n) = 2!$

c.  $P(n, 2) = 2!$

b.  $C(n, n) = 1$

d. None of these

12. The value of  $C(5, 2)$  is

a. 5

c. 15

b. 10

d. 20

13. The proposition  $(p \rightarrow \sim p) \rightarrow \sim p$  is

a. Tautology

c. Either tautology or contradiction

b. Contradiction

d. None of these

14. If  $p$  is true, then the truth value of  $p \wedge \sim p$  will be

a. T

c. Cannot be said

b. F

d. None of these

15. For the sequence  $4, 12, 36, \dots$ , the recurrence relation is

a.  $a_{n+1} = 2$

c.  $a_{n+1} = 3a_n$

b.  $a_{n+1} = a_n$

d. None of these

16. Which of the following is not true

a. A cyclic group is always abelian

c. In a ring  $R$ ,  $(R, +)$  is a group

b. The identity in a group is unique

d. None of these

17. The dual of  $p \vee T \equiv T$  is

a.  $p \vee T \equiv F$

c.  $p \wedge T \equiv T$

b.  $p \vee F \equiv F$

d.  $p \wedge F \equiv F$

18. Which of the following is not a group

a.  $(\mathbb{R}, \cdot)$

c.  $(\mathbb{R}, +)$

b.  $(\mathbb{Z}, +)$

d. None of these

19. A poset  $(L, \leq)$  is called lattice if every pair of elements in  $L$  has

a. Supremum

c. Both supremum and infimum

b. Infimum

d. Neither supremum nor infimum

20. An ordered arrangement of  $r$  elements of a set containing  $n$  distinct elements is called a/an

a.  $r$ - permutation of  $n$  elements

c. Pigeonhole principle

b.  $r$ -combination of  $n$  elements

d. None of these

( PART-B : Descriptive )

Time : 2 hrs. 40 min.

Marks : 50

[ Answer question no.1 & any four (4) from the rest ]

1. a. Define conditional and biconditional propositions and also give the truth tables. 6+4=10

b. What is equivalence of propositions. Show that  $(p \rightarrow q) \leftrightarrow \sim p \vee q$ .

2. a. Define group with an example. 4+6=10

b. Show that the set  $Q^+$  of all positive rational numbers forms an abelian group under the operation  $*$  defined by  $a * b = \frac{1}{2}ab$ ;  $a, b \in Q^+$ .

3. If  $S = \{1, 2, 3, 4, 5\}$  and if the function  $f, g, h: S \rightarrow S$  are given by: 4+3+3=10

$f = \{(1, 2), (2, 1), (3, 4), (4, 5), (5, 3)\}$

$g = \{(1, 3), (2, 5), (3, 1), (4, 2), (5, 4)\}$

$h = \{(1, 2), (2, 2), (3, 4), (4, 3), (5, 1)\}$

(Here  $(a, b) \in f \Rightarrow f(b) = a$ ,  $(p, q) \in g \Rightarrow g(q) = p$   $(x, y) \in h \Rightarrow h(y) = x$ )

a. Verify whether  $f \circ g = g \circ f$ .

b. Explain why  $f$  and  $g$  have inverse but  $h$  does not.

c. Find  $f^{-1}$  and  $g^{-1}$ .

4. If  $f: \mathbb{Z} \rightarrow \mathbb{N}$  is defined by  $f(x) = \begin{cases} 2x - 1, & \text{if } x > 0 \\ -2x, & \text{if } x \leq 0 \end{cases}$  6+4=10

a. Prove that  $f$  is one-one and onto

b. Determine  $f^{-1}$ .

5. a. Define Decomposition of a graph. Prove that - A graph containing  $m$  edges  $\{e_1, e_2, \dots, e_m\}$  can be decomposed into  $2^{m-1} - 1$  different ways into pairs subgraphs  $G_1$  and  $G_2$ . 6+4=10

b. Define Complete Graph, Regular Graph and Planer Graph.

6. a. State Handshaking theorem. A graph consists of four vertices each of degree  $m$  and an isolated vertex. Find the number of edge of the graph. 2+4+4=10

b. Find adjacent matrix and incident matrix of the following graph:

