Time: 2 hrs. 40 min. Marks: 50

[Answer question no.1 & any four (4) from the rest]

- 1. Derive an expression for frequency of plasma oscillation. In presence of thermal motion, the plasma oscillations propagate. Hence, write down the dispersion relation of electron plasma wave.
- 2. **a.** Find an expression for the grad-B drift of a gyrating particle in a nonuniform magnetic field. Also discuss the trajectory of the charged particles.
 - **b.** An electron and an ion of masses m_e and m_i respectively are subjected to a constant and uniform magnetic field \vec{B} . Show that the kinetic energy acquired by an electron in time τ is m_i/m_e times greater than the kinetic energy acquired by an ion. Assume, the average time τ between two collisions is the same for electrons and ions.
- 3. a. In a magnetic mirror, the trajectory of a charged particle makes an angle θ_0 with the magnetic field line. Show that the mirror ratio R_m is given by $\frac{1}{R_m} = \frac{B_0}{B_m} = \sin^2 \theta_m.$ Here B_0 is the strength of the magnetic field at the centre and B_m is the strength of the magnetic field at the throat of the magnetic mirror system.
 - b. A plasma with an isotropic velocity distribution is placed in a magnetic mirror trap with mirror ratio $R_m = 2$. Find the value of pitch angle θ_m .
- 4. **a.** What do you mean by Debye shielding length of plasma? Compute the Debye length of earth's ionosphere with typical value of temperature $T = 10^3$ K and number density $n = 10^{12}$ m⁻³
 - **b.** Starting from electromagnetic field tensor $F^{\mu\nu}$, derive Maxwell's second equation.
- 5. a. What is the power radiated by a point charge? 4+6=10
 - **b.** Show that the power radiated from a electric dipole varies as the fourth power of the frequency.
- 6. a. Explain retarded potentials? 6+4 =10
- b. Obtain the expressions for the famous Liénard-Wiechert potentials.
- 7. **a.** Discuss the reflection and transmission of the electromagnetic waves at oblique incidence and obtain the Snell's law.
 - b. Describe the theory of propagation of electromagnetic waves inside a rectangular waveguide of uniform cross section.
- 8. a. What are the static and dynamic Maxwells equations? Derive the equation of continuity. 3+3+4
 - b. Write a short note on Cherenkov radiation.
 - c. Prove the uniqueness theorems in electrostatics.

REV-00 MSP/57/62

M. Sc. PHYSICS SECOND SEMESTER

ELECTROMAGNETICS & PLASMA PHYSICS

MSP-201

(Use Separate Answer Scripts for Objective & Descriptive)

Duration: 3 hrs. Full Marks: 70

(PART-A: Objective)

Time: 20 min. Marks: 20

Choose the correct answer from the following:

1×20=20

- 1. A charged particle in a constant and uniform electric field \vec{E} where |B|=0 describes a
 - a. motion with constant velocity
 - b. uniformly accelerated motion
 - c gyrated motion with constant radius
 - d. periodic motion with constant amplitude.
- **2.** If λ_D is the Debye length and L is the dimension of plasma, then which of the following represents the criterion of an ionized gas to behave as plasma?
 - a. $\lambda_D \ll L$

b. $\lambda_D \gg L$

c. $\lambda_D \approx L$

- d. $\lambda_D = \sqrt{L}$
- 3. The cyclotron frequency of electron in a homogeneous magnetic field of 0.1 Tesla is

a.
$$\omega_c = 1.76 \times 10^{10} \, \text{Hz}$$

b.
$$\omega_c = 1.758 \times 10^{12} \,\mathrm{Hz}$$

c.
$$\omega_c = 1.758 \times 10^9 \text{ Hz}$$

d.
$$\omega_c = 1.76 \times 10^{11} \text{ Hz}$$

4. The $\vec{E} \times \vec{B}$ drift velocity for the motion of a non-relativistic charged particle in the presence of crossed electric (E) and magnetic (B) fields which are constant in time and uniform in space is expressed as

$$\mathbf{a.} \ \overrightarrow{v_E} = \frac{\vec{E}. \ \vec{B}}{\mathbf{P}^2}$$

$$\mathbf{b.} \overrightarrow{v_E} = \frac{q}{\underline{m}} \frac{\overrightarrow{E} \times \overrightarrow{B}}{\underline{B}^2}$$

$$\mathbf{c.} \ \overrightarrow{v_E} = \frac{mv_\parallel^2}{2} \frac{\overrightarrow{E} \times \overrightarrow{B}}{B^2}$$

$$\mathbf{d.} \overrightarrow{v_E} = \frac{\overrightarrow{E} \times \overrightarrow{B}}{B^2}$$

- 5. Drift of a gyrating particle in crossed gravitational and magnetic fields depends on the ratio
 - a. $\frac{mv_{\parallel}^2}{q}$

b. $\frac{2mv_{\perp}^2}{q}$

 $c, \frac{m}{q}$

 $\frac{d}{m}$

6. For an electron plasma wave, if v_{th} is thermal velocity of electrons the phase velocity vph is always greater than or equal to

a.
$$\sqrt{3/2} v_{th}$$

b.
$$\sqrt{1/3} v_{th}$$

d. v_{th}^2

d.
$$v_{th}^2$$

7. The magnitude of the magnetic moment $|\vec{\mu}|$ associated with the circulating current of charged particle in a uniform magnetostatic field \vec{B} can be expressed as

$$\mathbf{a.} \ |\vec{\mu}| = \frac{1}{2} m \omega_c$$

$$\mathbf{b.} |\vec{\mu}| = \frac{1}{2} \omega_c r_c$$

c.
$$|\vec{\mu}| = \frac{|\vec{q}|}{2} \omega_c r_c^2$$

$$\mathbf{d.} |\vec{\mu}| = \frac{|q|}{2} \omega_c r_c^2$$

The number of atoms in a Debye sphere N_D is related to the Debye shielding length λ_D as

a.
$$N_D \propto \sqrt{\lambda_D}$$

c. $N_D \propto 1/\lambda_D^3$

b.
$$N_D \propto \lambda_D^3$$

d.
$$N_D \propto \lambda_D$$

9. The four momentum of a particle at rest having mass m is

$$\mathbf{a.} \ p^{\mu} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$$\mathbf{b.} \ p^{\mu} = \begin{pmatrix} mc^2 \\ 0 \\ 0 \\ pc \end{pmatrix}$$

$$\mathbf{c.} \ p^{\mu} = \begin{pmatrix} mc^2 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$$\mathbf{d.} \quad p^{\mu} = \begin{pmatrix} me^2 \\ p_x e \\ p_y e \\ p_z e \end{pmatrix}$$

10. Relativistic version of continuity equation is expressed as, where I^{μ} is the current density

$$\mathbf{a.} \ \partial_{\mu}J^{\mu} = -\frac{\rho}{\epsilon_0}$$

$$\mathbf{b.}\ \partial_{\mu}J^{\mu}=0$$

$$\mathbf{c.}\ \partial_{\mu}^{2}J^{\mu}=0$$

$$\mathbf{d.}\ \partial_{\mu}J^{\mu}=-\mu_{0}\epsilon_{0}$$

- 11. Accelerating electric charges produce
 - a. Electric field

b. Electromagnetic waves

c. Electric and magnetic field

- d. None of these
- 12. The fields which survives at large distances from the source is called
 - a. Radiation zone

- b. Electromagnetic field
- c. Both Radiation zone and Electromagnetic field
- d. None of these
- 13. The energy transported by an electromagnetic wave is called the

- b. Poynting vector
- c. Energy flux
- d. Intensity

a.
$$v = \frac{\omega}{\kappa}$$
c. $v = \frac{2\omega}{\kappa}$

$$v = \frac{d\omega}{d\kappa}$$

$$v = \frac{\kappa}{2\omega}$$

15. Choose the incorrect option

a.
$$v = \frac{c}{n}$$

b.
$$v = \frac{\sqrt{\epsilon \mu}}{\sqrt{\epsilon_0 \mu_0}}$$

$$c. \quad v = \frac{\sqrt{\epsilon \mu}}{\sqrt{\epsilon_0 \mu_0}}$$

$$d. \ v = \frac{1}{\sqrt{\epsilon \mu}}$$

Opt out the incorrect option

$$\mathbf{a} \cdot \vec{k} \times \vec{E} = \omega \, \vec{B}$$

$$\mathbf{b} \cdot \vec{E} = \frac{\omega}{k} \vec{B}$$

c.
$$k^2 = \frac{c^2}{v^2}$$

$$\mathbf{d}.\,\vec{E} = \hat{C}\,\vec{B}$$

- 17. Electromagnetic field is
 - a. conservative

b. discontinuous

c. non- conservative

- d. none of these
- 18. The potential inside an enclosure completely surrounded by conducting material, provided there is no charge within the conductor is
 - a. unity

b. zero

c. constant

- d. undefined
- 19. The Rayleigh scattering intensity for a single particle varies inversely as the
 - a. First power of wavelength
- b. second power of wavelength
- c. Third power of wavelength
- d. Fourth power of wavelength
- 20. The tangential component of electric field at the boundary must be
 - a continuous

b. undefined

c. discontinuous

d. Fourth power of wavelength