

M.Sc. PHYSICS
FIRST SEMESTER
ELECTRODYNAMICS
MSP – 104

**SET
A**

[USE OMR FOR OBJECTIVE PART]

Duration: 1:30 hrs.

Full Marks: 35

Time: 15 mins.

(Objective)

Marks: 10

Choose the correct answer from the following:

1×10=10

- Which one of the following Maxwell's equations implies the absence of magnetic monopoles?
 - $\nabla \cdot \mathbf{E} = \rho/\epsilon_0$
 - $\nabla \cdot \mathbf{B} = 0$
 - $\nabla \times \mathbf{E} = -\partial \mathbf{B}/\partial t$
 - $\nabla \times \mathbf{B} = (\frac{1}{c^2}) \partial \mathbf{B}/\partial t + \mu_0 \mathbf{j}$
- The gauge transformation of the scalar and vector potentials that leave the electric and magnetic field invariant are:
 - $\vec{A} \rightarrow \vec{A}' = \vec{A} - \frac{\partial \lambda}{\partial t}$
 $\mathbf{V} \rightarrow \mathbf{V}' = \mathbf{V} + \nabla \lambda$
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 $\mathbf{V} \rightarrow \mathbf{V}' = \mathbf{V} + \frac{\partial \lambda}{\partial t}$
- An electro-magnetic field is defined by a scalar potential $V(\vec{r}, t) = 0$ and vector potential $\vec{A}(\vec{r}, t) = \frac{1}{4\pi\epsilon_0} \frac{q\vec{r}}{r^2} \hat{r}$. The corresponding electric field is:
 - $\vec{E} = 0$
 - $\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$
 - $\vec{E} = -\frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$
 - $\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{\theta}$
- For a medium of electric and magnetic field, the relation between E and B with propagation vector k is:
 - $\vec{E} \times \vec{k} = \omega \vec{B}$
 - $\vec{E} \times \vec{k} = \vec{\omega} \times \vec{B}$
 - $\vec{E} = \frac{\vec{k}}{\omega} \times \vec{B}$
 - $\vec{B} = \frac{\vec{k} \times \vec{E}}{\omega}$
- Current flowing in a circuit containing a capacitor, to satisfy the continuity equation $\vec{\nabla} \cdot \vec{j} = -\frac{\partial \rho}{\partial t}$, for charge and current, the current density \vec{j} must be replaced by
 - $\epsilon_0 \frac{\partial \vec{E}}{\partial t}$
 - $\vec{j} - \epsilon_0 \frac{\partial \vec{E}}{\partial t}$
 - $\vec{E} - \epsilon_0 \frac{\partial \vec{j}}{\partial t}$
 - $\vec{j} + \epsilon_0 \frac{\partial \vec{E}}{\partial t}$

6. If electric field $\vec{E}=E\hat{x}$ and magnetic field $\vec{B}=B\hat{y}$, then the Poynting vector can be expressed as:
- | | |
|--|--|
| a. $\vec{S} = \epsilon_0 E^2 \hat{z}$ | b. $\vec{S} = c\epsilon_0 E^2 \hat{z}$ |
| c. $\vec{S} = c\epsilon_0 E^2 \hat{y}$ | d. $\vec{S} = c\epsilon_0 E^2 \hat{x}$ |
7. What should be the velocity of a charge particle moving through a velocity selector? (V, B and E represent the velocity, magnetic field and electric field intensities respectively)
- | | |
|------------|------------------|
| a. $V=B/E$ | b. $V=E/B$ |
| c. $V=EB$ | d. None of above |
8. Which of the following parameter is invariant under Lorentz transformation?
- | | |
|----------------------------|----------------------------|
| a. $\vec{E} \cdot \vec{B}$ | b. $\vec{E} \cdot \vec{A}$ |
| c. $\vec{E} \cdot \vec{M}$ | d. $\vec{E} \cdot \vec{P}$ |
9. For accelerated charge particle; the electric field (E) varies with distance r is
- | | |
|------------------------------|------------------------------|
| a. $E \propto \frac{1}{r^3}$ | b. $E \propto \frac{1}{r^4}$ |
| c. $E \propto \frac{1}{r}$ | d. $E \propto \frac{1}{r^2}$ |
10. The medium used in Michelson-Morley experiment is
- | | |
|-----------|----------|
| a. Aether | b. Water |
| c. Glass | d. Gas |

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(Descriptive)

Time : 1 hr. 15 mins.

Marks: 25

[Answer question no.1 & any two (2) from the rest]

1. State maxwell's electromagnetic equations for free space and hence prove that the velocity of an electromagnetic wave is equal to the speed of light. 2+3=5

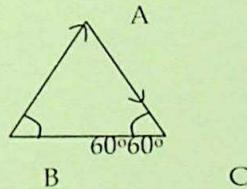
2. The electric field of an electromagnetic wave is given by $\vec{E} = (10\hat{y} + 5\hat{z})\cos [\omega t + (2y - 4z)]$. Find (i) k , (ii) ω , (iii) \vec{B} and (iv) J_d (the symbols have their usual meanings) 2+2+4+2=10

3. Using the Lorentz gauge condition $\nabla \cdot A + \mu_0 \epsilon_0 \frac{\partial V}{\partial t} = 0$, prove that $\square^2 V = -\frac{\rho}{\epsilon_0}$ and $\square^2 A = -\mu_0 J$ 5+5= 10

4. An infinite straight wire carries current $I(t) = 0$ for $t \leq 0$ 5+5=10
 $= I_0$ for $t > 0$
Find the retarded vector potential and electric field at a distance s from the wire.

5. State the Lorentz transformation equations in special theory of relativity. Two persons A and B are moving with equal speed $c/2$ as shown in the figure. What is the velocity of B with respect to A? 4+6=10

$c/2$ $c/2$



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